



## Outcome 1 - The Product Rule with basic functions

### Worked Example:

Differentiate  $y = x^3 \sin x$

1. Define the functions.

Let  $y = uv$  where  $u = x^3$  and  $v = \sin x$

2. Differentiate both functions.

$$\frac{du}{dx} = 3x^2 \quad \frac{dv}{dx} = \cos x$$

3. Find  $\frac{dy}{dx}$ .

$$\frac{dy}{dx} = x^3 \cos x + 3x^2 \sin x$$

#### Key Facts/Formulae:

The product rule enables us to differentiate a function consisting of two other functions that are multiplied together.

E.g. If  $y = uv$ , then  $\frac{dy}{dx} = u \frac{dv}{dx} + v \frac{du}{dx}$

#### Essential prior knowledge!

$$f(x) = \sin x \quad f'(x) = \cos x$$

$$f(x) = \cos x \quad f'(x) = -\sin x$$

### Questions...

Differentiate each of the following with respect to  $x$ .

1

$$y = x \sin x$$

2

$$y = 6x^2 \cos x$$

3

$$y = 2x^3 \cos x$$

4

$$y = x^5 \sin x$$

5

$$y = 2x^{10} \cos x$$

6

$$y = \frac{1}{2}x^6 \sin x$$

# Answers

**1**

$$\frac{dy}{dx} = x \cos x + \sin x$$

**2**

$$\frac{dy}{dx} = -6x^2 \sin x + 12x \sin x$$

**3**

$$\frac{dy}{dx} = -2x^3 \sin x + 6x^2 \cos x$$

**4**

$$\frac{dy}{dx} = x^5 \cos x + 5x^4 \sin x$$

**5**

$$\frac{dy}{dx} = -2x^{10} \sin x + 20x^9 \cos x$$

**6**

$$\frac{dy}{dx} = -\frac{1}{2}x^6 \cos x + 3x^5 \sin x$$