

Outcome 1 - Completing the Square

Bronze examples...

Examples...

Write the following quadratics in the form...

$$y = (x + a)^2 + b.$$

$$y = x^2 + 8x + 4$$

**** half the coefficient of x! ****

$$= (x + 4)^2 + 4 - 16$$

$$= (x + 4)^2 - 12$$

**** square it and take it away! ****

$$y = x^2 - 2x - 10$$

$$= (x - 1)^2 - 10 - 1$$

$$= (x - 1)^2 - 11$$

Silver example

Examples...

Write the following quadratics in the form...

$$y = (x + a)^2 + b.$$

$$y = x^2 + 7x + 3$$

**** half the coefficient of x! ****

$$= (x + \frac{7}{2})^2 + 3 - \frac{49}{4}$$

**** square it and take it away! ****

$$= (x + \frac{7}{2})^2 - \frac{37}{4}$$

Gold example

Examples...

Write the following quadratics in form...

$$y = a(x + b)^2 + c.$$

$$y = 2x^2 + 12x + 7$$

**** common factor first! ****

$$= 2(x^2 + 6x) + 7$$

**** Then complete the square as normal! ****

$$= 2(x + 3)^2 + 7 - 18$$

$$= 2(x + 4)^2 - 11$$

**** Don't forget to multiply! ****

Bronze Questions

Write the following quadratics in the form...

$$y = (x + a)^2 + b.$$

 $y = x^2 + 8x + 5$  $y = x^2 + 10x + 10$

 $y = x^2 + 2x - 7$  $y = x^2 + 4x + 3$

 $y = x^2 + 6x - 2$  $y = x^2 - 12x + 15$



 $y = x^2 - 2x + 14$  $y = x^2 - 8x + 1$

 $y = x^2 - 6x - 9$  $y = x^2 - 14x + 40$

Silver Questions

Write the following quadratics in the form...

$$y = (x + a)^2 + b.$$

 $y = x^2 + 5x + 7$  $y = x^2 + 13x + 22$

 $y = x^2 + x - 10$  $y = x^2 + 7x + 26$

 $y = x^2 + 3x - 6$  $y = x^2 - 11x + 17$



 $y = x^2 - x + 29$  $y = x^2 - 3x + 5$

 $y = x^2 - 9x - 15$  $y = x^2 - 17x + 38$

Gold Questions



Write the following quadratics in the form...

$$y = a(x + b)^2 + c.$$

 $y = 3x^2 + 12x + 2$  $y = 2x^2 + 16x + 3$

 $y = 4x^2 + 16x - 7$  $y = 3x^2 + 24x - 11$

 $y = 2x^2 + 28x - 5$  $y = 3x^2 - 36x + 8$

 $y = 9x^2 - 18x + 19$  $y = 2x^2 - 4x + 25$

 $y = 8x^2 - 32x - 7$  $y = 2x^2 - 14x + 5$

Bronze Answers

1. $y = (x + 4)^2 - 11$
2. $y = (x + 5)^2 - 15$
3. $y = (x + 1)^2 - 8$
4. $y = (x + 2)^2 - 1$
5. $y = (x + 3)^2 - 11$
6. $y = (x - 6)^2 - 21$
7. $y = (x - 1)^2 + 13$
8. $y = (x - 4)^2 - 15$
9. $y = (x - 3)^2 - 18$
10. $y = (x - 7)^2 - 9$

Silver Answers

1. $y = (x + 5/2)^2 + 3/4$
2. $y = (x + 13/2)^2 - 81/4$
3. $y = (x + 1/2)^2 - 41/4$
4. $y = (x + 7/2)^2 + 55/4$
5. $y = (x + 3/2)^2 - 33/4$
6. $y = (x - 11/2)^2 - 53/4$
7. $y = (x - 1/2)^2 + 115/4$
8. $y = (x - 3/2)^2 + 11/4$
9. $y = (x - 9/2)^2 - 141/4$
10. $y = (x - 17/2)^2 - 137/4$

Gold Answers

1. $y = 3(x + 2)^2 - 10$
2. $y = 2(x + 4)^2 - 29$
3. $y = 4(x + 2)^2 - 23$
4. $y = 3(x + 4)^2 - 59$
5. $y = 2(x + 7)^2 - 103$
6. $y = 3(x - 6)^2 - 100$
7. $y = 9(x - 1)^2 + 10$
8. $y = 2(x - 1)^2 + 23$
9. $y = 8(x - 2)^2 - 39$
10. $y = 2(x - 7/2)^2 + 3/2$